

# FER – Teaching complex concepts



**AQUILONIS d.o.o.**

SREDNJA EKONOMSKA ŠOLA  
IN GIMNAZIJA MARIBOR



**SVEUČILIŠTE U ZAGREBU**  
**FAKULTET ELEKTROTEHNIKE I RAČUNARSTVA**

**TARTU KUTSEHARIDUSKESKUS**  
**ZAVOD ANTONA MARTINA SLOMŠKA MARIBOR**



AGENCIJA ZA  
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## ACTIVE LEARNING THROUGH IMPROVED INTERACTIVITY

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# Context

- University of Zagreb, Faculty of electrical engineering and computing
- 1st semester graduate elective course with ~50 students  
*Digital signal processing*



# Motivation

- Contents include:
- time discrete signals and Fourier transformation
- introduction to DSP and digital filters
- continuous time-domain filters
- design of Finite Impulse Response (FIR) filters
- design of Infinite Impulse Response (IIR) filters
- Fast Fourier Transform (FFT)
- ...

# Methods

- *Ex chatedra teaching*  
*theoretical concepts*
- *Problem solving sessions*  
*exam problems*
- *Laboratory sessions*  
*practical implications*



# Example – Drawing the DTFT spectrum

- To plot the DTFT spectrum of a discrete-time aperiodic signal  $x[n]$ :
  1. find the DTFT transformation of the signal  $X(e^{j\omega})$
  2. find the magnitude spectrum  $|X(e^{j\omega})|$
  3. find the phase spectrum  $\angle X(e^{j\omega})$
  4. plot them separately on the  $[-\pi, \pi]$  interval

# 1. Find the DTFT transformation

- Let  $x[n]$  be a discrete-time aperiodic signal
- Its DTFT is calculated as

$$X(e^{j\omega}) = \sum_{n=-\infty}^{\infty} x[n]e^{-j\omega n}$$

# 1. Find the DTFT transformation

- For example, if  $x[n] = [\underline{1}, 2, 1]$

its DTFT is calculated as

$$X(e^{j\omega}) = \sum_{n=-\infty}^{\infty} x[n]e^{-j\omega n} = 1 + 2e^{-j\omega} + 1e^{-2j\omega}$$

## 2. Find the magnitude spectrum $|X(e^{j\omega})|$

- Calculate the magnitude spectrum  $|X(e^{j\omega})|$
- Use (a)symmetry to reduce the expression to sinus and cosinus if possible

## 2. Find the magnitude spectrum $|X(e^{j\omega})|$

- For example, the magnitude spectrum of signal  $x[n]$

$$\begin{aligned}|X(e^{j\omega})| &= |1 + 2e^{-j\omega} + e^{-2j\omega}| \\&= |e^{-j\omega}| \cdot |e^{j\omega} + 2 + e^{-j\omega}| \\&= |2 + 2\cos(\omega)| = 2|1 + \cos(\omega)|\end{aligned}$$

### 3. Find the phase spectrum $\angle X(e^{j\omega})$

- Calculate the phase spectrum of  $x[n]$
- Unwrap the phase to  $[-\pi, \pi]$  interval if it exceeds it

*What is the phase of a real number?*

*What is the phase of an imaginary number?*

### 3. Find the phase spectrum $\angle X(e^{j\omega})$

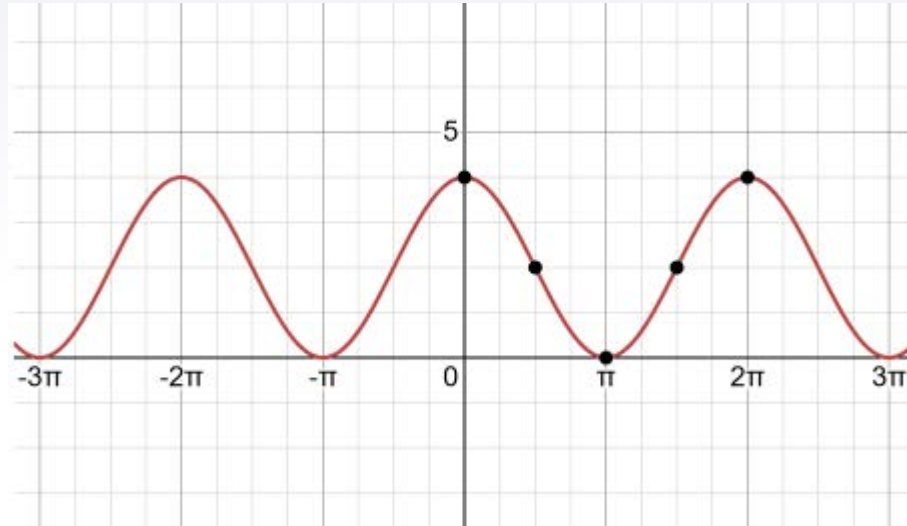
- For example, the phase spectrum of  $x[n]$  is

$$\begin{aligned}\angle X(e^{j\omega}) &= \angle(1 + 2e^{-j\omega} + e^{-2j\omega}) \\ &= \angle(e^{-j\omega}[2 + 2\cos(\omega)]) = -\omega + \angle[2 + 2\cos(\omega)] = -\omega\end{aligned}$$

## 4. Plot the spectrum on the $[-\pi, \pi]$ interval

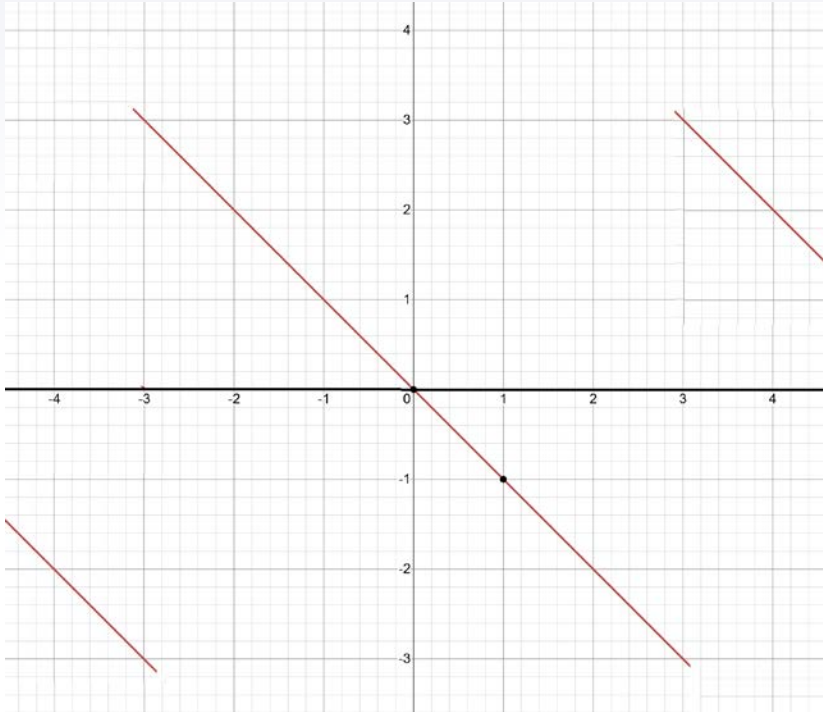
- Magnitude spectrum is always non-negative!
- Phase spectrum should be unwrapped to the  $[-\pi, \pi]$  interval on the y-axis

## 4. Amplitude spectrum $|X(e^{j\omega})|$



$$-|X(e^{j\omega})| = 2|1 + \cos(\omega)|$$

## 4. Phase spectrum $\angle X(e^{j\omega})$



$$- \quad \angle X(e^{j\omega}) = -\omega$$

# Issues

- *Poor prior knowledge (course prerequisite!)*
- *Poor working habits*

→ *The course has a reputation of being difficult among students*



# Thank you for your attention!